# **Clipped Projections for More Informative Visualizations** [a Work-in-Progress Report]

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- Plot with large scale lacks small-scale details (limited resolution)
- Zooming-in for details loses further away points
- Example: plotting the full 2D data (left) misses detailed structure



### **Find informative visualization**

- Specify a background model to be  $\mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{I})$ , with  $\sigma^2 = \text{Tr}(\hat{\mathbf{X}}'\hat{\mathbf{X}})/nd$
- Quantify information content:
- $IC(\mathbf{W}, \hat{\mathbf{\Pi}}_{\mathbf{W}}, \mathbf{c}) =$







 $\Pr(\hat{z} \in [l, u]) = p(\hat{z}) \cdot 2fc$ 

 $\mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{I})$ 

 $\rightarrow \mathbf{W}$ 

Can we balance scale and detail automatically?

#### **Idea of method**

- 1) Overlay bounding box on scatter plot
- 2) Clip points outside to border and present them with a different marker
- 3) Zoom-in to fill plotting area
- For points inside, we learn their position up to the **resolution**
- For points on the border, we learn their direction
- We can quantify the information content of this visualization

- $-\log \Pr\left(\hat{\mathbf{\Pi}}_{\mathbf{W}} \in \left[\mathbf{L}\left(\hat{\mathbf{\Pi}}_{\mathbf{W}}, \mathbf{c}
  ight), \mathbf{U}\left(\hat{\mathbf{\Pi}}_{\mathbf{W}}, \mathbf{c}
  ight)
  ight]
  ight)$
- Maximize the information content over W and c:



 $\Pr(\hat{z} \in [l, u]) = \int_{-\infty}^{-c} p(z) dz$ 

• Example: optimize c for 1 dimensional data sampled from Normal distribution  $\mathcal{N}(0,1)$  and Cauchy distribution f(0,1)







## **Clipped projection**

- Denote the 1D projection of data  $\hat{\mathbf{x}}_i \in \mathbb{R}^d$ onto  $\mathbf{w} \in \mathbb{R}^d (\mathbf{w}'\mathbf{w} = 1)$  point as  $\hat{z}_i = \hat{\mathbf{x}}'_i \mathbf{w}$
- A **bounding box** is a (centered) window (-c, c), with  $c \in \mathbb{R}_+$
- Idea: For a **resolution parameter** f,

projection  $\hat{z}_i$  is specified up to a **pixel** of size  $f \cdot 2c$ 



0

С

 $\hat{z}_i$  0

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0

 $\mathbf{W}$ 

 $ightarrow \mathbf{W}$ 

 $ightarrow \mathbf{W}$ 

#### **Case study: UCI segmentation dataset**

- Dataset:  $\hat{\mathbf{X}} \in \mathbb{R}^{210 \times 19}$ , 210 image patches (  $3 \times 3$  pixels) drawn randomly from a database of 7 outdoor images. Data points are described by 19 image features and are categorized into seven classes.
- **Results:** the principal components are dominated by a single outlier, while the clipped scatter plot shows variation in the center of the data.

